

Credit Based Third Semester B.C.A. Degree Examination, Nov./Dec. 2018

BASIC MATHEMATICS
(Common to All Batches)

Time : 3 Hours

Max. Marks : 80

Note : Answer **any ten** questions from Part – A and **any one full** question from **each** Unit in Part – B.

PART – A

(10×2=20)

1. a) Prove that $\log \frac{x}{y} + \log \frac{y}{z} + \log \frac{z}{x} = 0$.
- b) Find the value of x if
 - i) $\log_5 x = 3$ ii) $\log_a x = 0$.
- c) Find the centre and radius of the circle whose equation is $x^2 + y^2 - 4x + 8y - 5 = 0$.
- d) Find the limit of $\frac{4x^4 + 3x^2 - 1}{x^3 + 7}$ when $x = 1$ and $x = -1$.
- e) If $y = 2x + x^2$, what is $\frac{dy}{dx}$?
- f) Integrate : $3 - 2x - x^4$.
- g) $A = \{2, 4, 6, 7, 9\}$ $B = \{1, 2, 4, 7, 8\}$ find $A + B$.
- h) Represent $A \cap B$ and $\sim A$ using Venn diagram.
 - i) Define reflexive relation. Give example.
 - j) Define digraph. Give an example.
 - k) Define root and leaf nodes of a tree. Give an example.
 - l) Define a loop. Give an example.



PART - B

Unit - I

2. a) Prove that $\frac{\log\sqrt{27} + \log\sqrt{8} - \log\sqrt{125}}{\log 6 - \log 5} = \frac{3}{2}$.
- b) Find the middle term in the expansion of $\left(x - \frac{1}{2y}\right)^7$.
- c) Find the equation of tangent and normal to the circle $x^2 + y^2 - 6x + 8y + 17 = 0$ at $(1, -2)$. (5+5+5)
3. a) Evaluate $\log\frac{41}{35} + \log 70 - \log\frac{41}{2} + 2\log 5$.
- b) Find the coordinates of the point which divides internally and externally the line joining $(2, -4)$ and $(7, 1)$ in the ratio $2 : 3$.
- c) Show that $(4, -5)$ $(8, 1)$ $(14, -3)$ and $(10, -9)$ is a square. (5+5+5)

Unit - II

4. a) If $\sec\theta = \frac{13}{5}$ and θ is in the 4th quadrant, find the value of $\frac{13\sin\theta + 5\sec\theta}{5\tan\theta + 6\operatorname{cosec}\theta}$.
- b) Differentiate $9x^4 - 7x^3 + 8x^2 - \frac{8}{x} + \frac{10}{x^3}$ with respect to x .
- c) Prove that $4(\sin^4 30^\circ + \cos^4 60^\circ) - 3(\cos^2 45^\circ - \sin^2 90^\circ) - 2 = 0$. (5+5+5)
5. a) Prove that $\frac{(\sin 30^\circ + \cos 60^\circ)(\sin 0^\circ + \cot 45^\circ)(\cot 90^\circ + \tan 60^\circ)}{(\tan 45^\circ + \sec 60^\circ)(\operatorname{cosec} 30^\circ + \tan 0^\circ)} = \frac{1}{2\sqrt{3}}$.
- b) Evaluate $\lim_{x \rightarrow 2} \frac{2x^2 - 5x + 2}{x^2 - 3x + 2}$.
- c) Evaluate :
- i) $\int (4x^3 + 3x^2 - 2x + 5) dx$
- ii) $\int_6^{10} \left(\frac{dx}{(x+2)}\right)$. (5+5+5)



Unit - III

6. a) $R = \{ \langle 1, 1 \rangle, \langle 1, 2 \rangle, \langle 1, 4 \rangle, \langle 2, 1 \rangle, \langle 2, 2 \rangle, \langle 2, 3 \rangle, \langle 3, 2 \rangle, \langle 3, 3 \rangle, \langle 4, 2 \rangle, \langle 4, 4 \rangle \}$. Construct relation matrix of R and draw diagram of R.
- b) $A = \{1\}$ $B = \{a, b\}$ $C = \{2, 3\}$ write $A \times B$, $B \times A$, $A^2 \times B$, $A \times B \times C$, $C^2 \times A$.
- c) Define surjective, injective and Bijective functions with example. (5+5+5)

7. a) Let $X = \{1, 2, 3\}$ f, g, h and s are the functions from X to X given by

$f = \{ \langle 1, 2 \rangle, \langle 2, 3 \rangle, \langle 3, 1 \rangle \}$ $h = \{ \langle 1, 1 \rangle, \langle 2, 2 \rangle, \langle 3, 1 \rangle \}$

$g = \{ \langle 1, 2 \rangle, \langle 2, 1 \rangle, \langle 3, 3 \rangle \}$ $s = \{ \langle 1, 1 \rangle, \langle 2, 2 \rangle, \langle 3, 3 \rangle \}$

Find $f \circ g$, $g \circ f$, $s \circ s$, $f \circ h \circ g$, and $f \circ s$

- b) $A = \{x/x \text{ is an integer and } 0 \leq x \leq 5\}$, $B = \{3, 4, 5, 17\}$ and $C = \{1, 2, 3\}$

Find :

- i) $A \cup B$ ii) $A \cap B$
 iii) $A - B$ iv) $A - C$
 v) $A \cap C$.

- c) Given the relation matrices

$$M_R = \begin{vmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{vmatrix} \quad M_S = \begin{vmatrix} 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \end{vmatrix}$$

Find $M_{R \circ S}$, $M_{\bar{R}}$, $M_{\bar{S}}$, $M_{R \circ \bar{S}}$ and show that $M_{R \circ \bar{S}} = M_{\bar{S}} \circ M_{\bar{R}}$. (5+5+5)

Unit - IV

8. a) Define the following with a example for each :
- i) Simple path
 - ii) Null graph
 - iii) Cyclic graph.
- b) Explain path and reachability with suitable example.



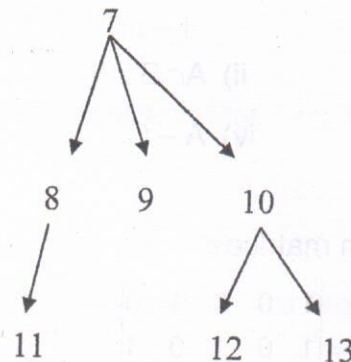
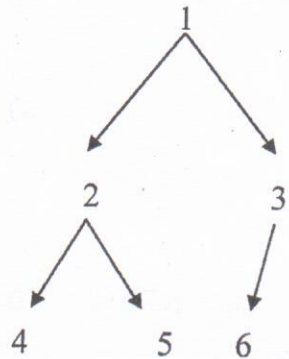
- c) $A = \{1, 2, 3, 4\}$ and R be a relation on A that has the matrix

$$M_R = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{pmatrix}$$

Construct relational graph of R and write in-degree and out-degrees of all the nodes.

(6+4+5)

9. a) What are strongly connected and weakly connected graphs? Explain with suitable examples.
- b) Define the following terms with example.
- out degree of node
 - length of a path.
- c) Convert the following into binary tree



(5+4+6)